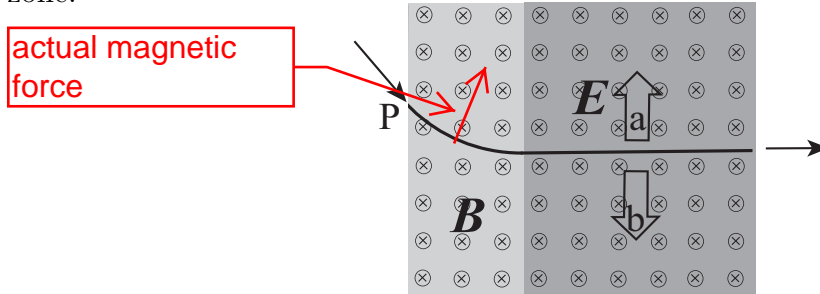


Name: \_\_\_\_\_ Section: \_\_\_\_\_ Score: \_\_\_\_\_/20

1. In the figure below a uniform magnetic field  $B$  perpendicular to the page is applied in gray zones, and a uniform electric field  $E$  perpendicular to  $B$  is applied in the darker gray zone.



(a) The injected charged particle rotates by 50 degrees in the pale gray zone, and then runs straight through the darker gray zone. Which is the correct uniform  $E$  field direction, a or b? You must justify your choice. [3]

Notice that this answer does NOT depend on the sign of the charge. So to solve this you may simply assume the charge is positive

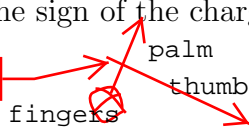
b to oppose the magnetic force upward (for a positive charge).

Try to do the same, assuming the charge is negative.

(b) What is the sign of the charge? [2]

The current and the velocity are in the same directions, so the charge must be positive.

the current direction



(c) The magnitude of the required magnetic field is 1.2 T and that of the electric field is 1.8 kV/m. What is the speed of the particle at P, the injection point? [5]

|magnetic force| =  $qvB$  (since  $v$  is perp to  $B$ )  
 |electric force| =  $qE$

They must agree.  $\rightarrow E = vB \rightarrow v = E/B = 1800/1.2 = 1500 \text{ m/s}$ .

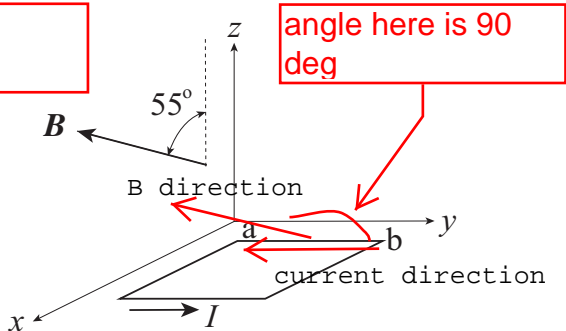
2. A metal square frame with edge 0.5 m lies in the  $xy$ -plane. A uniform magnetic field  $\mathbf{B}$  of magnitude 1.5 T is parallel to the  $xz$ -plane, making an angle  $55^\circ$  with the  $z$ -axis as illustrated below.

(a) The metal frame carries a permanent current of  $I = 2$  A in the direction of the arrow. What is the magnitude of the total force acting on the edge  $ab$ , which is parallel to the  $y$ -axis? [5]

Right-hand rule  
 magnitude:  $ILB \sin \theta$ , where the angle is between  $I$  and  $B$ .

Notice that in this case  $\theta = 90^\circ$

$$F = ILB = 2 \times 0.5 \times 1.5 = 1.5 \text{ N.}$$



(b) What is the magnitude of the torque on the square? [5]

$\tau = IAB \sin \theta$ , where  $\theta$  is the angle between  $B$  and the normal

The angle is  $55^\circ$ .

$$\tau = IAB \sin \theta$$

$$= 2 \times 0.5^2 \times 1.5 \times \sin 55 = 1.23 \text{ N.m.}$$

