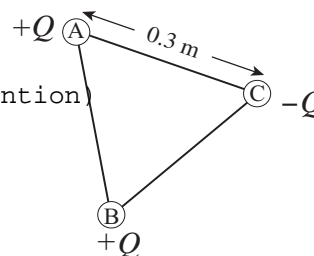


Name: \_\_\_\_\_ Section: \_\_\_\_\_ Score: \_\_\_\_\_/20

1. Three charges of  $+Q$ ,  $+Q$  and  $-Q$  ( $Q > 0$ ) are placed at the three vertices of equilateral triangle of edge length 0.3 m as shown below. The total work you have to do to construct this charge configuration from three charges apart far away from each other is  $-3.0$  J.

superposition  
pairwise potential energy  $kQQ'/r$

Total potential energy (according to our energy convention)  
 $kQ^2/r + kQ(-Q)/r + kQ(-Q)/r = -kQ^2/r = -3$  J.



(1) What is the magnitude of  $Q$ ? [5]

$$Q = \sqrt{3r/k} = \sqrt{0.9/9 \times 10^9} = \sqrt{10^{-10}} = 10^{-5} = 10 \text{ microC.}$$

(2) Now, you wish to remove charge B (move it far away from other charges). How much work do you have to do? [5]

Obviously 0, since AB and BC pairs store +3 and -3 J.

2. There are four charges on the plane. The equipotential curves are described in the following figure.

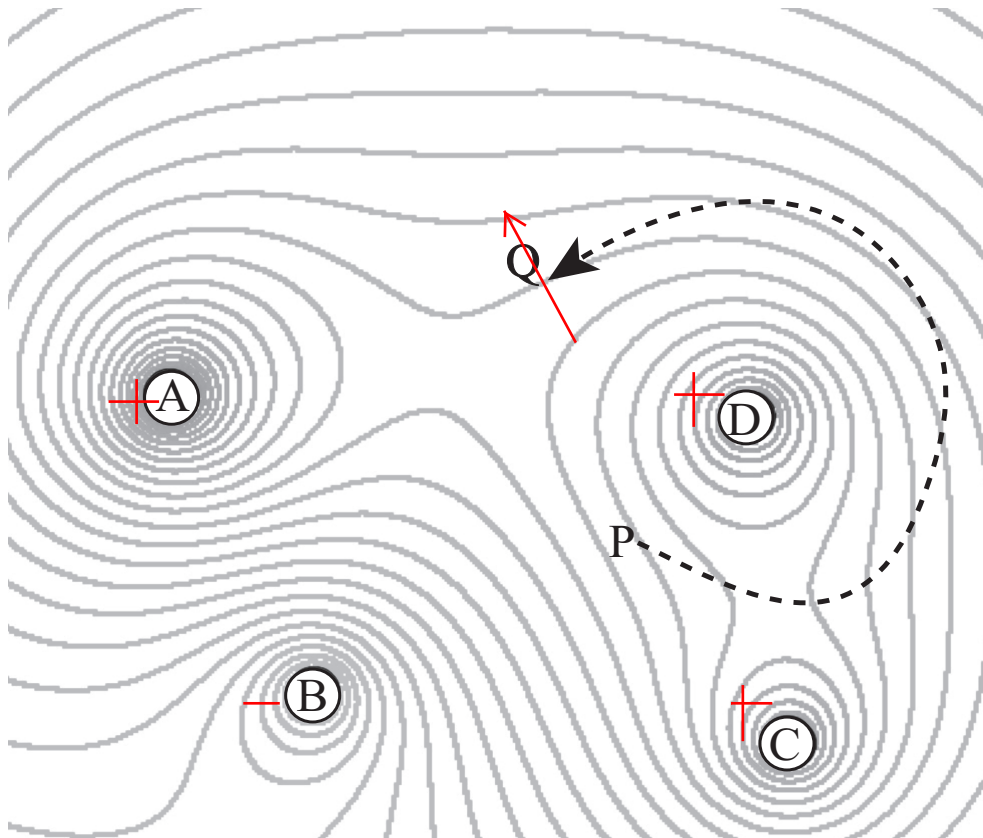


Figure 1:

(1) One charge has a different sign from the other three. What is this charge? [4]

B, because the other three are connected by a mountain ridge.

(2) Assume A is positive. Indicate the direction of the electric field at Q. You must justify your answer briefly. [2]?

+ is higher and E must be downhill, perpendicular to the contour at the point.

(3) If you move a charge of +1 C from P to Q, how much work  $W$  do you have to supply, if the contour spacing is 20 V? [ $W$  need not be positive.] [4]

$$W = q \times \Delta V$$

P has a higher voltage than Q by 20 V, so it is downhill, two spacings = 40 V down.  
 $W = 1 \times (-40) = -40 \text{ J}.$