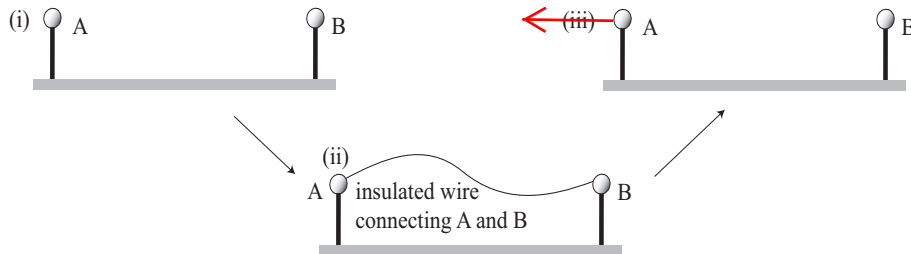


Name: _____ Section: _____ Score: _____/20

1 Very small identical metal spheres A and B are on glass stands placed as in the figure below (i). Initially, A has net charge nQ and B Q . The Coulomb force acting on charge A is \mathbf{F} . Then, A and B are connected by an uncharged (and insulated) metal wire as (ii) in the figure. After the wire is removed (iii), the force acting on charge A becomes \mathbf{F}' . The distance between the small spheres is kept constant. The ratio of the horizontal component (let us call it the x -component) of the forces is given as $F_x/F'_x = -3$.



(a) What is a very fundamental law (property) of charges we need to determine the charges on the spheres in (iii)? [2].

conservation of charge

Thus $(n+1)Q/2$ is on A and B, respectively.

(b) Find the initial ratio of the charge n (an integer) (no justification, no credit!) [6]

Coulomb's law

The x -component of the forces are:

Before: $F_x = k(nQ)(Q)/r^2$, where r is the distance between A and B,

After: $F'_x = k(n+1)^2 Q^2/4r^2$

so

$$F/F' = 4n/(n+1)^2 = -3.$$

or

$$3n^2 + 10n + 3 = (3n + 1)(n + 3) = 0.$$

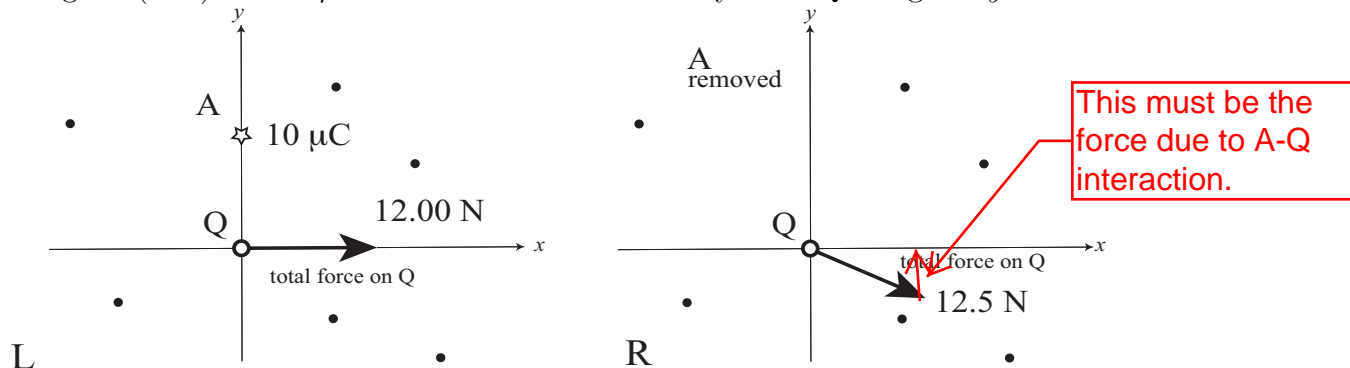
This implies $n = -3$.

If you write down this, you get almost a full score.

(c) Draw the direction of the Coulomb force acting on A in (iii) in the figure above [2]

The force must be repulsive.

2. There are several charges on a plane as shown (as dots and a star) in the figure below left (L). The total electrostatic force acting on charge Q at the origin is 12 N in the +x-direction. The charge A (star) is $+10 \mu\text{C}$ and is located 30 cm away from Q along the y-axis.



(a) When the charge at Q is doubled, what is the total electrostatic force acting on Q? [2]

Superposition + Coulomb

The total force is proportional to Q, so 24 N

When the charge A is removed (situation R in the figure above) but all the remaining charges are kept intact, the total electrostatic force acting on charge Q is 12.37 N with the direction in the figure.

(b) What is the sign of charge Q? You must state justification of your answer. [3]

Superposition + Coulomb

The red arrow must be the force on Q due to A.

Therefore, Q is attracted to A. A is positive, so Q must be negative.

(c) What is the magnitude of charge Q? You must state justification of your answer. [5]

The magnitude of the red arrow is, thanks to Pythagoras' theorem $\sqrt{12.5^2 - 12^2} = 3.5 \text{ N}$.

Using Coulomb's force (magnitude) formula $F = kQq'/r^2$, we get

$3.5 = 9 \times 10^9 \times Q \times (10 \times 10^{-6}) / 0.3^2$, BUT never do this. Solve Q first:

$Q = Fr^2/kQ'$.

Therefore,

$$Q = 3.5 \times (0.3^2) / (9 \times 10^9)(10 \times 10^{-6}) = 3.5 \times 10^{-2-9+5}$$

$$= 3.5 \times 10^{-6}$$

or 3.5 microC. (The charge is - 3.5 microC.)