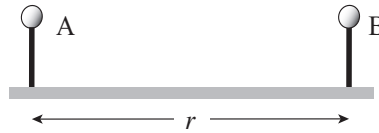


Name: _____ Section: _____ Score: _____/20

1. Very small metal spheres A and B are on glass stands placed r m apart as in Figure below.



(a) Initially, A and B have certain charges Q and Q' , and the electrostatic force between them is 12 N and repulsive. What is the force between them, if the AB distance is halved? [3].

Coulomb's force: $F = kQQ'/r^2 = 12 \text{ N}$.

If r is halved, then $F \rightarrow F' = kQQ'/(r/2)^2 = 4F = 48 \text{ N}$.

(b) What is the very fundamental law (property) of charges we need to determine the charges on the spheres after touching ? [2].

Charge conservation

(c) After A touches B, they are again isolated and placed r apart as shown in the figure. The magnitude of the force is 16 N. Obtain $x = Q/Q'$ (Assume $Q > Q'$). If you get the equation for x , you get the full credit. [5]

After touching the charges are both $(Q + Q')/2$, so the force after touching is $F' = k(Q+Q')^2/4r^2 = 16\text{N}$.

From F and F' we get (you may assume Q and Q' are positive thanks to the charge conjugation symmetry)

$$QQ' = 12r^2/k$$

$$(Q + Q')^2 = 64r^2/k$$

That is

$$(Q + Q')^2 = (64/12) QQ' = (16/3)QQ'$$

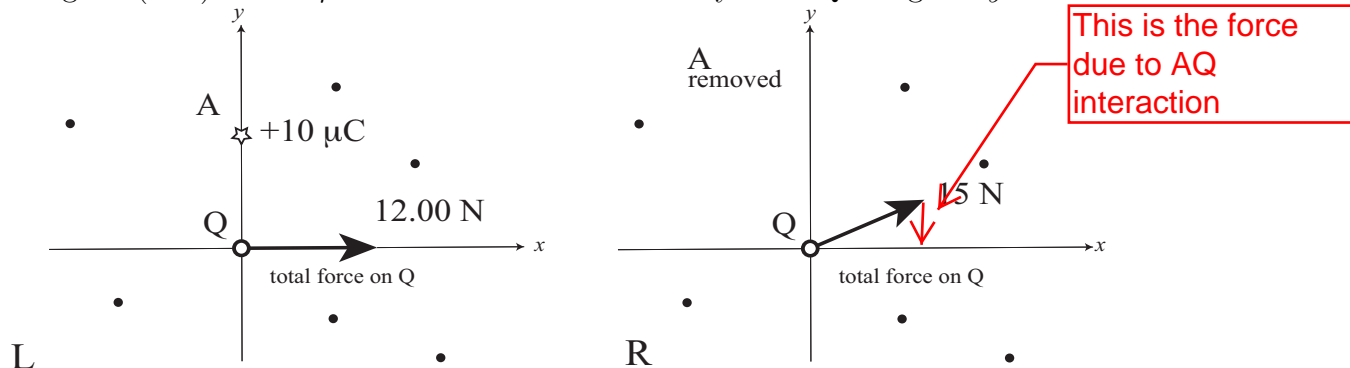
If we set $x = Q/Q'$, then

$$(x+1)^2 = (16/3)x.$$

This gives $x = 3$.

If you write this, you get almost a full score.

2. There are several charges on a plane as shown (as dots and a star) in the figure below left (L). The total electrostatic force acting on charge Q at the origin is 12 N in the +x-direction. The charge A (star) is $+10 \mu\text{C}$ and is located 30 cm away from Q along the y-axis.



(a) When the charge at Q is halved to $Q' = Q/2$, what is the total electrostatic force acting on Q? [2]

Superposition principle tells us that the total force is proportional to Q.

Hence, the total force is simply halved: 6 N.

When the charge at A is removed (situation R in the figure above) but all the remaining charges are kept intact, the total electrostatic force acting on charge Q becomes 15 N with the direction in the figure.

(b) What is the sign of charge Q? You must state justification of your answer. [3]

Pay attention to superposition principle

The difference is due to the removal of charge A. This increase the 'pull' in the direction of the location of A so the original force must have been repulsive. Q must have a positive charge.

(c) What is the magnitude of charge Q? You must exhibit your work neatly. [5]

The magnitude of the red arrow is, thanks to Pythagoras' theorem $\sqrt{15^2 - 12^2} = 9 \text{ N}$.

Using Coulomb's force (magnitude) formula $F = kQq'/r^2$, we get $9 = 9 \times 10^9 \times Q \times (5 \times 10^{-6}) / 0.3^2$, BUT never do this. Solve Q first:
 $Q = Fr^2/kq'$.

Therefore,

$$Q = 9 \times (0.3^2) / (9 \times 10^9)(10 \times 10^{-6}) = 9 \times 10^{-2-9+5}$$

$$= 9 \times 10^{-6}$$

or 9 microC.